

## Sections 5.2, 5.3 and 5.4

### I- Find the exact value of each expression

- 1)  $6 \cos \frac{3\pi}{4} + 2 \tan(-\frac{\pi}{3})$     2)  $\sec(-\frac{\pi}{3}) - \cot(-\frac{5\pi}{4})$     3)  $\cos(-\pi) - \sin(-\frac{3\pi}{2})$     4)  $2 \cot(-\frac{\pi}{6}) + \cos(-\frac{5\pi}{6})$   
5)  $\sin \frac{4\pi}{3} - 2 \tan \frac{11\pi}{6}$     6)  $\cot \frac{5\pi}{4} + \sec(-\frac{11\pi}{6})$     7)  $\csc(-\frac{2\pi}{3}) + \cos(\frac{7\pi}{6})$     8)  $\cot(-\frac{\pi}{2}) - \sin(-\frac{7\pi}{2})$   
9)  $\frac{\sin 50^\circ}{\cos 40^\circ} + \frac{1}{\cot^2(-40^\circ)}$     10)  $\sin 200^\circ \sec(-70^\circ)$     11)  $\cot 200^\circ \cot(-70^\circ)$     12)  $\frac{\tan^2 20^\circ \sin 70^\circ}{\sec 20^\circ}$   
13)  $1 + \tan^2 5^\circ - \csc^2 85^\circ$     14)  $\tan 350^\circ \cot 10^\circ$     15)  $\frac{1}{\cos 38^\circ \csc 52^\circ} - \csc 38^\circ \sec 52^\circ$   
16)  $\frac{\cos 40^\circ}{\sin(-320^\circ)} + \cot 140^\circ$     17)  $\sec 35^\circ \csc 55^\circ - \tan 35^\circ \cot 55^\circ$     18)  $\sin 160^\circ \cos 70^\circ - \cos 20^\circ \sin 290^\circ$   
19)  $\tan(-120^\circ) - \sin(-210^\circ)$     20)  $4 \csc(-\frac{5\pi}{3}) - 3 \tan(-\frac{7\pi}{6})$     21)  $\cot \frac{7\pi}{6} + \cos(-\frac{2\pi}{3})$     22)  $3 \cos \frac{5\pi}{6} - \cot \frac{\pi}{3}$   
23)  $\frac{\sin^2 \frac{\pi}{6} - \cos \frac{\pi}{3}}{\cos \frac{\pi}{4}}$     24)  $\frac{2(\sin^2 \frac{\pi}{3}) - \cos^2 \frac{\pi}{4}}{\tan \frac{\pi}{3}}$     25)  $\frac{2 \sin \frac{4\pi}{3} - \tan \frac{11\pi}{6}}{2 \cos(-\pi) - \sin(-\frac{3\pi}{2})}$     26)  $\frac{\csc \frac{3\pi}{4} - \cot \frac{7\pi}{4}}{\sin(-\frac{\pi}{2}) - \sec \frac{5\pi}{4}}$

### II- Answer true or false

- 1)  $\sin 270^\circ + \cos(-180^\circ) = 0$     2)  $\sin(-\pi) = -1$     3)  $\tan(-\frac{3\pi}{2})$  is undefined    4)  $\cos(-360^\circ) - \sin(-90^\circ) = 2$   
5)  $\cos(\frac{2\pi}{3}) = \cos(-\frac{\pi}{3})$     6)  $\sin(\frac{6\pi}{5}) = \sin(-\frac{\pi}{5})$     7)  $\tan(\frac{5\pi}{6}) = \cot(-\frac{\pi}{3})$     8)  $\csc(-\frac{7\pi}{6}) = \sec(\frac{5\pi}{3})$   
9)  $\cos(-\frac{3\pi}{4}) = \sin(\frac{7\pi}{4})$     10)  $\cos(\frac{6\pi}{7}) = \cos(-\frac{\pi}{7})$     11)  $\tan(\frac{9\pi}{8}) = \cot(\frac{\pi}{2} - \frac{\pi}{8})$     12)  $\cot 270^\circ + \cos 0^\circ = 0$   
13)  $\cot(-\pi)$  is undefined    14)  $\csc(-270^\circ) + \sec(-180^\circ) = 0$     15)  $\sec(\frac{\pi}{2}) - \sin(\frac{3\pi}{2}) = 1$     16)  $\sin(\pi - \frac{\pi}{9}) = \sin(\frac{\pi}{9})$   
17)  $\tan(360^\circ - 30^\circ) = -\tan 30^\circ$     18)  $\cos(\frac{\pi}{4} - 2\pi) = -\cos \frac{\pi}{4}$     19)  $\sin(\frac{\pi}{5} - 2\pi) = \sin \frac{\pi}{5}$     20)  $\cos(-5\pi) = -1$

### III- Find the exact values of each of the remaining Trig. functions given

- 1)  $\sec \theta = -\frac{5}{4}$  ,  $\tan \theta < 0$     2)  $\csc \theta = -4$  ,  $\pi < \theta < \frac{3\pi}{2}$     3)  $\sin \theta = -\frac{1}{3}$  ,  $\cos \theta > 0$   
4)  $\cot \theta = \frac{\sqrt{2}}{2}$  ,  $\sec \theta < 0$

- IV- 1) If  $\sec \theta = 3$  , find a)  $\cos \theta$  , b)  $\tan^2 \theta$  , c)  $\csc(90^\circ - \theta)$  , d)  $\sin^2 \theta$   
2) If  $\cot \theta = 2$  , find a)  $\tan \theta$  , b)  $\csc^2 \theta$  , c)  $\tan(90^\circ - \theta)$  , d)  $\sec^2 \theta$   
3) If  $\sin \theta = 0.3$  , find  $\csc \theta + \cos(90^\circ - \theta) + \sin(360^\circ - \theta)$   
4) If  $\cos \theta = 0.2$  , find  $\cos(-\theta) + \cos(2\pi - \theta) + \cos(\pi + \theta) + \cos(3\pi - \theta)$   
5) If  $\cot \theta = -2$  , find  $\cot(-\theta) + \cot(\theta - \pi) + \cot(2\pi - \theta) + \tan(\theta - \frac{\pi}{2})$

V- Evaluate the following :

1)  $\tan^2\left(-\frac{11\pi}{6}\right) - \sin^2\left(-\frac{7\pi}{18}\right) - \sin^2\left(\frac{\pi}{9}\right)$

2)  $\csc^2\left(-\frac{5\pi}{3}\right) + \tan^2\left(\frac{5\pi}{18}\right) - \csc^2\left(-\frac{2\pi}{9}\right)$

3)  $\sec^2\left(-\frac{13\pi}{7}\right) - \tan^2\left(-\frac{8\pi}{7}\right) - \cot^2\left(-\frac{5\pi}{6}\right)$

4)  $\cos^2\left(-\frac{5\pi}{3}\right) - \csc^2\left(-\frac{5\pi}{4}\right) + \sin^2\left(-\frac{2\pi}{3}\right)$

5)  $\csc\left(\frac{11\pi}{6}\right) + \cos\left(-\frac{\pi}{4}\right) - \sec(-3\pi)$

6)  $\tan\left(-\frac{5\pi}{6}\right) - \sec\left(-\frac{\pi}{6}\right) - \cos\left(-\frac{7\pi}{2}\right)$

7)  $\sec\left(-\frac{2\pi}{3}\right) + \cot\left(-\frac{\pi}{6}\right) - \sin\left(\frac{11\pi}{2}\right)$

VI) Evaluate the following expressions using Trig. Identities, assuming that  $0 < \theta < \frac{\pi}{2}$

1) If  $x = \frac{3}{2} \sin \theta$ , find  $\frac{x}{\sqrt{9 - 4x^2}}$

2) If  $x = a \sec \theta$ , find  $\frac{\sqrt{x^2 - a^2}}{x}$

3) If  $x = \sqrt{2} \cot \theta$ , find  $\frac{x}{\sqrt{2 + x^2}}$

- VII) 1) If  $p(x, -\frac{\sqrt{2}}{3})$  is on the unit circle such that  $x > 0$ , find  $\cot \theta$  where  $p$  is on the terminal side of the angle of  $\theta$  radians.
- 2) If  $p(-\frac{\sqrt{5}}{6}, y)$  is on the unit circle such that  $y < 0$ , find  $\csc \theta$  where  $p$  is on the terminal side of the angle of  $\theta$  radians.
- 3) If  $\csc \theta = -\frac{2}{\sqrt{3}}$ , find all possible values for  $\theta$  for  $0 \leq \theta < 2\pi$
- 4) If  $\tan \theta = \frac{1}{\sqrt{3}}$ , find all possible values for  $\theta$  for  $0 \leq \theta < 2\pi$
- 5) If  $\cos \theta = 0$ , find all possible values for  $\theta$  for  $0 \leq \theta < 2\pi$
- 6) If  $\cot \theta$  is undefined, find all possible values for  $\theta$  for  $0 \leq \theta < 2\pi$
- 7) If  $\cos \theta = -\frac{1}{2}$ , find all possible values for  $\theta$  for  $-2\pi \leq \theta < -\pi$
- 8) If  $\tan \theta = -\frac{1}{\sqrt{3}}$ , find all possible values for  $\theta$  for  $-\frac{3\pi}{2} \leq \theta < 0$
- 9) If  $\cot \theta = 0$ , find all possible values for  $\theta$  for  $-2\pi \leq \theta < -\frac{\pi}{2}$
- 10) If  $\csc \theta$  is undefined, find all possible values for  $\theta$  for  $-2\pi < \theta \leq \frac{\pi}{2}$
- 11) Find the y coordinate of  $p(x, y)$  on the unit circle and on the terminal side of the angle  $-\frac{5\pi}{3}$
- 12) Find the x coordinate of  $p(x, y)$  on the unit circle and on the terminal side of the angle  $-\frac{5\pi}{6}$
- 13) Suppose that the terminal point determined by  $\theta$ , is the point  $(\frac{2}{\sqrt{29}}, \frac{5}{\sqrt{29}})$  on the unit circle. Find the terminal point determined by  $5\pi + \theta$ .
- 14) Suppose that the terminal point determined by  $\theta$ , is the point  $(\frac{2}{\sqrt{29}}, \frac{5}{\sqrt{29}})$  on the unit circle. Find the terminal point determined by  $-\theta - 7\pi$ .

15) Suppose that the terminal point determined by  $\pi - \theta$ , is the point  $(-\frac{3}{\sqrt{34}}, \frac{5}{\sqrt{34}})$  on the unit circle. Find the terminal point determined by  $8\pi - \theta$ .

16) If  $\theta$  is an acute angle and the terminal side is determined by  $\theta$ , then the terminal side determined by  $3\pi - \theta$  will be in quadrant.

17) If  $\theta$  is an acute angle and the terminal side is determined by  $\theta$ , then the terminal side determined by  $\frac{11\pi}{2} + \theta$  will be in quadrant.