

Define *Euler's trilogarithm* by the series

$$\text{Li}_3(z) = \sum_{k=1}^{\infty} \frac{z^k}{k^3}$$

for $|z| < 1$. Observe that $\text{Li}'_3(z) = \frac{\text{Li}_2(z)}{z}$.

1. Use the above to define a function element (D, Li_3) where D is a (sufficiently) small disc centered at $1/2$.
2. Starting at $z = 1/2$, compute the analytic continuation Li_3^γ of Li_3 , still in a neighborhood of $1/2$, where γ is the curve:
 - (a) winding once around the point $z = 0$;
 - (b) winding once around the point $z = 1$.