

Suppose that $f(z)$ is holomorphic on the closed unit disc, and it satisfies $|f(z)| \leq 1$ for all $z \in \mathbb{D}$. Also assume that $f(1/3) = f(i/3) = 0$, and f vanishes nowhere else in the closed unit disc. Provide an estimate for $|f(0)|$.