Let $f$ be a complex harmonic function on a connected open set $U$. Suppose $f^{2}$ is also harmonic. Prove that either $f$ or $\bar{f}$ is holomorphic.

