

Quiz 2 (front and back)

Name: KEYN

1. Let $\mathbf{a} = \mathbf{i} - \mathbf{j} - \mathbf{k}$ and $\mathbf{b} = 2\mathbf{i} - \mathbf{j} + 4\mathbf{k}$.

(a) Find the cross product $\mathbf{a} \times \mathbf{b}$.

$$\langle -5, -6, 1 \rangle$$

(b) Find the equation of the line parallel to $\mathbf{a} \times \mathbf{b}$ and through the point $(-1, 4, 3)$.

$$x = -1 - 5t$$

$$y = 4 - 6t$$

$$z = 3 + t$$

2. Let $\mathbf{r}(t) = \langle e^{\sin t}, \cos(\cos t), 1 - t^{-1} \rangle$. Find each of the following:

Note: These quantities may or may not exist. If something doesn't exist, state that and then clearly explain why.

(a) The domain of \mathbf{r} .

$$t \neq 0$$

(b) $\lim_{t \rightarrow 0} \mathbf{r}(t)$. does not exist:

$$\lim_{t \rightarrow 0^-} 1 - \frac{1}{t} = \infty \quad \text{but}$$

$$\lim_{t \rightarrow 0^+} 1 - \frac{1}{t} = -\infty.$$

(c) The unit tangent vector at $t = \pi$.

$$\vec{r}'(t) = \left\langle \cos t e^{\sin t}, -\sin(\cos t) \cdot -\sin t, \frac{1}{t^2} \right\rangle$$

$$\Rightarrow \vec{r}'(\pi) = \left\langle -1, 0, \frac{1}{\pi^2} \right\rangle$$

$$\Rightarrow \text{unit tangent vector is } \frac{\vec{r}'(\pi)}{|\vec{r}'(\pi)|} = \frac{\left\langle -1, 0, \frac{1}{\pi^2} \right\rangle}{\sqrt{1 + \frac{1}{\pi^4}}}$$