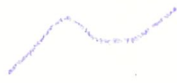


DN: The crossing number of a path is the number of times it comes back to a vertex it has already been to.

Ex



CRN = 3



CRN = 0



CRN = 3

DN A SIMPLE PATH is one that does not repeat any vertex. (i.e. its crossing number is zero)

Thm A: If there is a path  $x \rightarrow y$  in  $G$ , then there is a simple path  $x \rightarrow y$  in  $G$ .

Corr B: In a tree every path is a simple path.

DN: A TOUR is a sequence of vertices  $x_0, x_1, \dots, x_n$  so that  $x_k$  is adjacent to  $x_{k+1}$  for  $0 \leq k < n$ . (i.e. a path that can repeat edges).

DN The revisit number of a ~~path~~<sup>tour</sup> is the number of times it comes back to an edge it has already been to. (Note a tour with  $rev\ n = 0$  is a path)

Thm C: If there is a tour  $x \rightarrow y$  in  $G$ , then there is a path  $x \rightarrow y$  in  $G$ .

Corr D If there is a tour  $x \rightarrow y$  in  $G$ , then there is a simple path  $x \rightarrow y$  in  $G$

TEST PROBLEM \*7 Prove Thm A, Corr B, Thm C & Corr D  
Hint: Prove Thm A (resp Thm C) by induction on the CRN (resp RV No)