

- other side

13. FOR  $\vec{X}(t) = \sin t \vec{i} + \cos t \vec{j} + e^t \vec{k}$ , FIND FOR ALL  $t$  THE VELOCITY, SPEED, ACCELERATION AND  $\vec{T}$
14. BEFORE STARTING THIS PROBLEM SUBSTITUTE  $t=0$  IN THE EQUATIONS OF \*13 TO OBTAIN  $\vec{X}(0)$ ,  $\vec{X}'(0)$ ,  $|\vec{X}'(0)|$ ,  $\vec{X}''(0)$ ,  $\vec{T}(0)$ , USING THESE VECTORS (OR ANY OTHER METHOD) FIND AT  $t=0$   $\vec{A}_T$ ,  $\vec{A}_N$ ,  $\vec{N}$  &  $\vec{B}$ .
15. AGAIN USING THE VECTORS AT THE START OF \*14 (OR ANY OTHER METHOD) FIND AT  $t=0$  THE SCALAR  $K$ , THE RADIUS OF CURVATURE, THE EQUATION OF THE TANGENT LINE AND THE EQUATION OF THE KISSING PLANE
16. FIND THE MIN & MAX VALUES OF  $f(x,y) = x^2 + y^2 - 2x - 2y$  IN THE CLOSED REGION  $x^2 + y^2 \leq 8$  [HINT TO CHECK THE BOUNDARY CHANGE  $f$  TO POLAR CO-ORDINATES SO  $r \leq 2\sqrt{2}$ ].
17. & 18:  $l_1: \vec{X} = (4\vec{i} + \vec{k}) + s(2\vec{i} - 2\vec{j} - \vec{k})$   $l_2: \vec{X} = (-\vec{i} + \vec{j} + \vec{k}) + t(\vec{i} - \vec{k})$
17. USING VECTOR METHOD'S, FIND THE DISTANCE BETWEEN  $l_1$  &  $l_2$
18. USING CALCULUS, FIND THE CO-ORDINATES OF THE POINT ON EACH LINE NEAREST THE OTHER.
19. FIND THE EQUATION OF THE PLANE  $P$  IF
- (i)  $P$  IS PARALLEL TO THE TANGENT PLANE OF  $z = x^3 + 2xy + y^2$  AT  $(1, 1)$  and
- (ii)  $P$  PASSES THROUGH THE POINT  $Q$  WHERE  $Q$  IS
- (a) ON THE TANGENT LINE TO THE CURVE  $\vec{X} = \vec{i} + t\vec{j} + \frac{t^2}{2}\vec{k}$  AT  $t=0$  and
- (b) ON THE PLANE  $x + y + z = 3$ .
20. THE FUNCTION  $f(x,y) = x^3 + xy^2 - 9x$  HAS 4 CRITICAL POINTS, FIND THEM AND USE THE SECOND DERIVATION TEST ON EACH TWO DETERMINE IF IT IS REL. MIN, REL. MAX, SADDLE, OR THE TEST FAILS. [HINT  $f_y$  FACTORS].

HAVE A MERRY & A HAPPY