$\qquad$

Directions: Show ALL work for credit; Give EXACT answers when possible; SIMPLIFY your answers;

1. Fill in the table below. The classification of the equation goes into the row labeled type. The characteristics go into the rows labeled $\Phi$ and $\Psi$. And the new variables are either $\xi$ (text uses $v$ ) and $\eta$ (text uses $w$ ) are in terms of $x$ and $y$. The normal form is in partials with respect to $\xi$ and $\eta$.

| PDE | $u_{x x}+9 u_{y y}$ | $u_{x x}-u_{x y}$ | $u_{x x}+u_{x y}-6 u_{y y}$ |
| ---: | :---: | :--- | :--- |
| type |  |  |  |
| $\Phi=$ |  |  |  |
| $\Psi=$ |  |  |  |
| $\xi=$ |  |  |  |
| $\eta=$ |  |  |  |
| Normal form |  |  |  |
|  |  |  |  |

