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Directions: Show ALL work for credit; Give EXACT answers when possible; SIMPLIFY your answers;

1. Find the Fourier series solution (and not D'Alembert's) $u=u(x, t)$ for the vibrating string of length $L=1$ and $c^{2}=1$ when the initial velocity is zero and the initial deflection is given by the function $f(x)=0.588 \sin (\pi x)-0.339 \sin (3 \pi x)+0.0642 \sin (5 \pi x)$ which is graphed below left. Sketch the graph of $u(x, 1 / 4)$ on the graph to the below right. [Hint: Two things, the series solution and the graph.]


