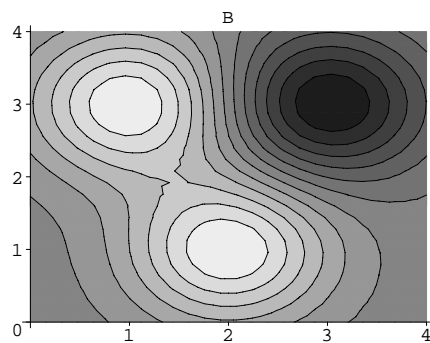
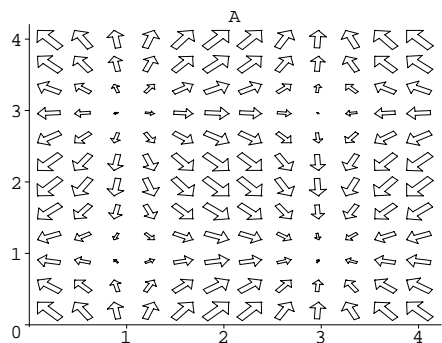
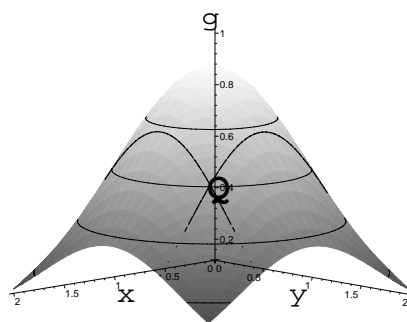
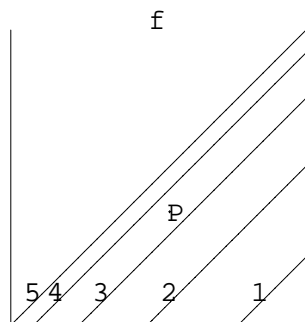


Show **ALL** work for credit; be neat; and use only **ONE** side of each page of paper. Do **NOT** write on this page. Calculators can be used for graphing and calculating only. Give exact answers when possible.

- Use the Chain Rule to find $\partial z/\partial u$ and $\partial z/\partial v$ when $z = \sin(x/y)$, $x = \ln u$ and $y = u^2 - v^2$.
- Fixing Maple errors. Each of the following produced an error or an empty graph, explain how to fix each.
 - `plot3d(exp^x*sin(y),x=0..1,y=0..2*Pi);`
 - `plot3d(x^2-x*y+y^2,x=0..1,y=1..1);`
 - `f=sin(x)*y^2+x^2*sin(y);plot3d(f,x=-1..1,y=-1..1);`
 - `plot3d(x y,x=-1..1,y=-1..1);`
 - `plot3d(sin(x)*sin(y),x=0..pi,y=0..pi);`
- For the function $f(x, y) = x^3 + xy + y^2$
 - Compute the quadratic Taylor polynomial for f at the point $(-1, 2)$.
 - Compute the equation of the normal line to f at the point $(-1, 2)$.
- The graph A is a plot of ∇f , the gradient of f and the graph B is a contourplot of g . (Light regions have higher values than dark regions.) Find the co-ordinates of all extrema of f and g and **LABEL** them as either local minimums, local maximums or saddle points.

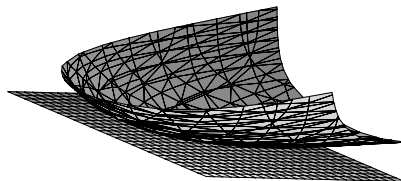


- Find the directional derivative of $f(x, y, z) = 3x^2y^2 + 2yz$ as you leave the point $(1, -1, 0)$ heading in the direction of the point $(0, 1, 1)$.
- The point P is on the contour graph of the function f (below left) and the point Q is on the surface of the graph of the function g (below right). Let \mathbf{u} be the unit vector $\mathbf{u} = (-\mathbf{i} - \mathbf{j})/\sqrt{2}$.
Find the sign (positive, negative or zero) of the partials of f : $f_x(P), f_y(P), f_{xx}(P), f_{yy}(P), f_{xy}(P)$ and the partials of g : $g_x(Q), g_y(Q), g_{xx}(Q)$ and the two directional derivatives $f_{\mathbf{u}}(P)$ and $g_{\mathbf{u}}(Q)$.



There is more test on the back.

Tangent Plane



7. Check that the point $(-1, 1, 2)$ lies on the surface $\cos(x + y) = e^{xz+2}$ and find the equation of the tangent plane to this surface at $(x, y, z) = (-1, 1, 2)$
8. Sketch the region of integration, reverse the order of integration and evaluate

$$\int_0^1 \int_{e^x}^e \frac{y}{\ln y} dy dx$$

9. Find critical points of the function $f(x, y) = (x + y)(x^2 + y^2 - 2)$. Classify these local extrema by filling out a table like the one below, with a separate line for each critical point. [Hint: Use your TI-89 to check that you got the correct collection of critical points.]

(x, y)	f_{xx}	f_{yy}	f_{xy}	big D	Classification
?	?	?	?	?	?

10. Use your TI-89 to plot the $z = 1$ contour of the function $z = g(x, y) = x^2 + xy + y^2$. On the same graph, plot some contour lines for $f(x, y) = x + y$. Use Lagrange Multipliers to find the maximum and minimum **VALUES** for $f(x, y)$ on the constraint $g(x, y) = 1$.