

Section 5.4

Review reference angles

Example 1: Find the reference angle for

a) $2\pi/3$

b) $-7\pi/4$

Example 2: Find the exact values for

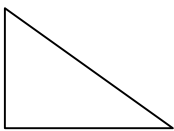
a) $\csc(3\pi/4)$

b) $\tan(-\pi/3)$

c) $\cos(300^\circ)$

Cofunctions

Recall: In a right triangle the two acute angles are complementary; i.e. the sum of their measures is 90° .



Cofunction identities

If A and B are complementary:

$$\sin A = \cos B$$

$$\tan A = \cot B$$

$$\sec A = \csc B$$

Written another way:

$$\sin \theta = \cos (\pi/2 - \theta)$$

$$\tan \theta = \cot (\pi/2 - \theta)$$

$$\sec \theta = \csc (\pi/2 - \theta)$$

$$\cos \theta = \sin (\pi/2 - \theta)$$

$$\cot \theta = \tan (\pi/2 - \theta)$$

$$\csc \theta = \sec (\pi/2 - \theta)$$

Example 3: If $\sin \theta = 4/5$ and θ is acute, find the exact value of $\cos (\pi/2 - \theta)$.

Review Pythagorean Identities

Example 4: Find the exact value of $\frac{\sec 70^\circ}{\csc 20^\circ} + \tan^2 20^\circ$.

Example 5: Select ALL the correct choices, if θ is acute and $\csc \theta = 5/2$

- a) $\sec^2 \theta = 21/25$
- b) $\cot^2 \theta = 4/21$
- c) $\sec (\pi/2 - \theta) = -2/5$
- d) none of these is correct

Example 6: Select ALL the correct choices

- a) $\cos(-\pi/6) = \csc(\pi/3)$
- b) $\tan(-\pi/4) = -\cot(\pi/4)$
- c) $\sin(3\pi/4) = \sin(-\pi/4)$
- d) none of these is correct

Example 7: Find the exact value of $\sec 15^\circ + \frac{1}{\sin 75^\circ} =$ (there are two possible answers)

Example 8: Select ALL the correct choices

a) $\csc \theta = \frac{\sqrt{3}}{2}$

b) $\cos \theta = \frac{1}{\sqrt{3}}$

c) $\cot \theta = \frac{1}{2}$

d) none of these is correct

